

**AGH University of Science and Technology**  
**Kraków**  
**Department of Strength & Fatigue of Material & Structures**

**Laboratory exercises**

**PHOTOELASTIC ANALYSES**

Faculty: .....

Year of study ..... Group No .....

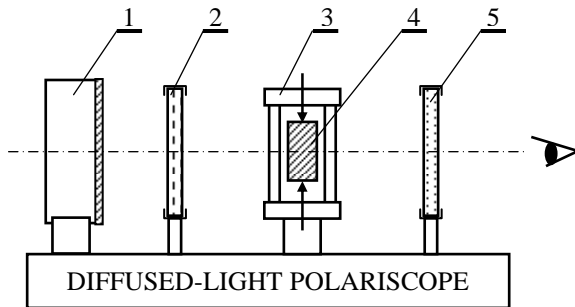
Date of exercise ..... Mark:.....

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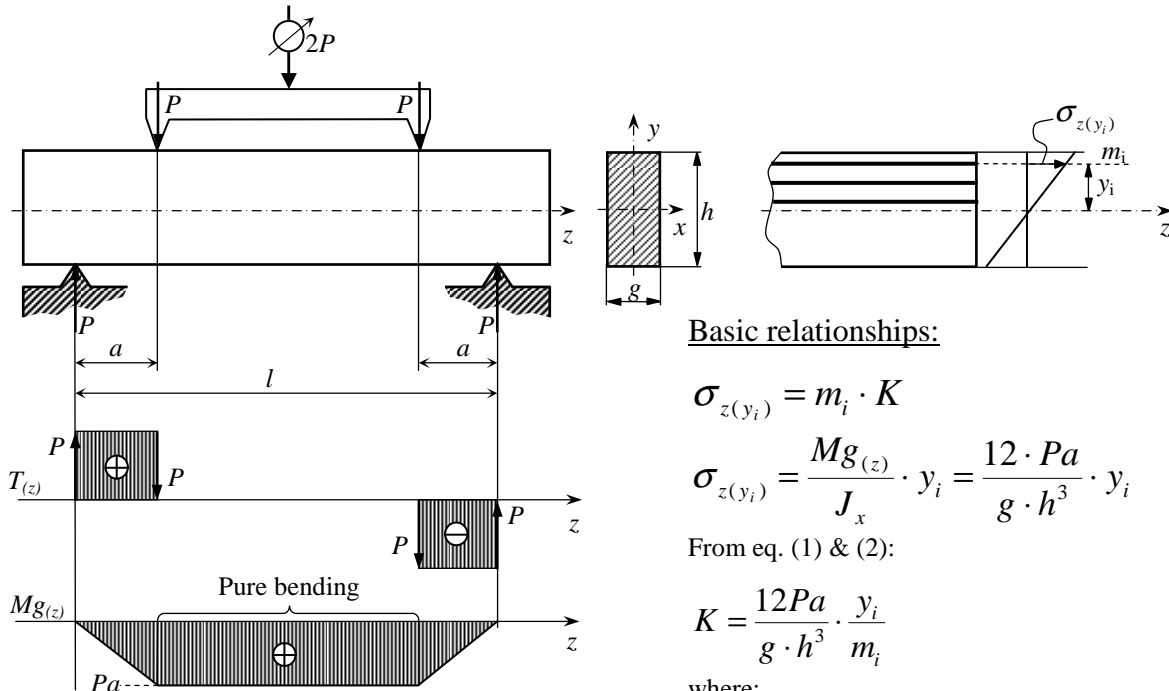
**Task No. 1.A: Determination of the constant of the photoelastic model based on isochromatic fringe pattern observed on a beam loaded by pure bending.**

1) The test stand diagram:



- 1 – source of light
- 2 – polarizer
- 3 – load frame
- 4 – tested specimen
- 5 – analyzer

2) The loading diagram:



**Basic relationships:**

$$\sigma_{z(y_i)} = m_i \cdot K \tag{A1}$$

$$\sigma_{z(y_i)} = \frac{Mg_{(z)}}{J_x} \cdot y_i = \frac{12 \cdot Pa}{g \cdot h^3} \cdot y_i \tag{A2}$$

From eq. (1) & (2):

$$K = \frac{12Pa}{g \cdot h^3} \cdot \frac{y_i}{m_i} \tag{A3}$$

where:

$y_i$  – coordinate of the  $m_i$  order isochromatic fringe  
 $K$  – constant of the photoelastic model

3) Dimensions of the specimen:

$h = \dots\dots\dots$  mm       $g = \dots\dots\dots$  mm       $l = \dots\dots\dots$  mm       $a = \dots\dots\dots$  mm

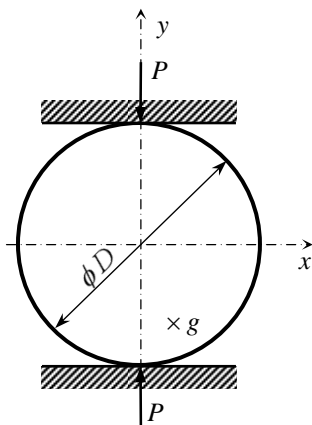
Force gage factor:       $k = \dots\dots\dots$  N/scale,

4) Experimental and calculation results:

Load level		Isochromatic fringe order $m_i$	Coordinate of $m_i$ – order isochromatic fringe	Constant of the photoelastic model
$2P$ , (scale)	$2P$ , (N)		$y_i$ , (mm)	
$K_{av} =$				

**Task No. 1.B: Determination of constant of the photoelastic model based on isochromatic fringe pattern observed on a compressed circular disc.**

1) The loading diagram:



2) Basic relationships:

a) Stresses in the center of disc:

$$\sigma_x = \frac{2P}{\pi g D}; \quad \sigma_y = -\frac{6P}{\pi g D}; \quad (B1)$$

$$\sigma_1 - \sigma_2 = \sigma_x - \sigma_y = \frac{8P}{\pi g D}; \quad (B2)$$

b) Stress-optic law:

$$\sigma_1 - \sigma_2 = m \cdot K; \quad (B3)$$

c) Model stress-optical coefficient for the circular disc (compare to eq. B2 – B3):

$$K = \frac{8P}{\pi g D m}; \quad (B4)$$

where:

$D, g$  – disk dimensions (see on the figure)

$m$  – isochromatic fringe order in the center of the disc

3) Dimensions of the disc:

$D = \dots\dots\dots$  mm

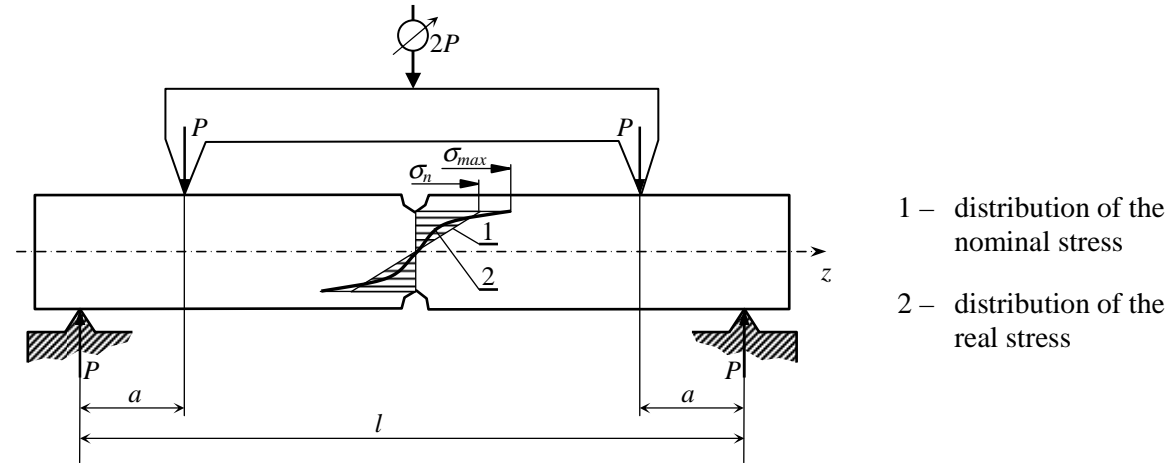
$g = \dots\dots\dots$  mm

4) Experimental and calculation results:

Load level		Isochromatic fringe order in the center of disc $m_i$	constant of the photoelastic model
$P$ , (scale)	$P$ , (N)		$K$ , (MPa)
$K_{av} =$			

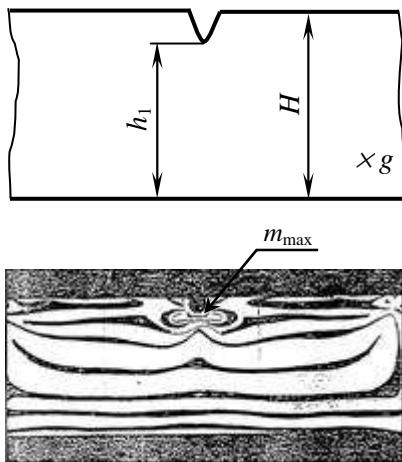
**Task No. 2: Determination of the stress concentration factor ( $k_t$ ) for the loaded by pure bending beam with single and double notch.**

1) The loading diagram:

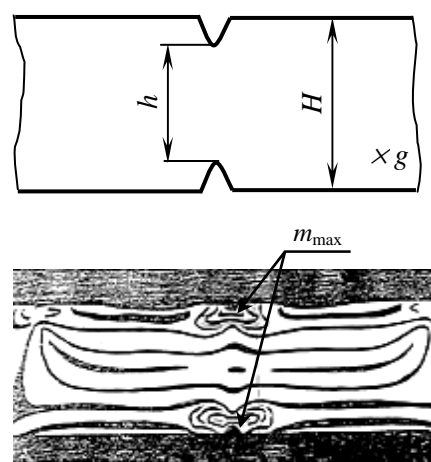


2) Considered specimens:

a) Model I  
The single-notch beam:



b) Model II  
The double-notch beam:



3) Basic relationships:

a) Stress concentration factor  $k_t$  (definition):

$$k_t = \frac{\sigma_{\max}}{\sigma_n}; \quad (2.1)$$

b) Maximum stresses at the notch tip  $\sigma_{\max}$ :

$$\sigma_{\max} = K \cdot m_{\max}; \quad (2.2)$$

where:  $m_{\max}$  – maximum isochromatic fringe order observed at the notch tip  
 $K$  – constant of the photoelastic model – assume  $K=K_{av}$  (acc. to Task No. 1.A)

c) Nominal stresses  $\sigma_n$ :

Model I:

$$\sigma_n = \frac{M_g}{W_{g\text{ netto}}} = \frac{6Pa}{gh_1^2}; \quad (2.3a)$$

Model II:

$$\sigma_n = \frac{M_g}{W_{g\text{ netto}}} = \frac{6Pa}{gh^2}; \quad (2.3b)$$

4) Specimens' dimensions:

$l = \dots\dots\dots$  mm       $a = \dots\dots\dots$  mm       $H = \dots\dots\dots$  mm       $g = \dots\dots\dots$  mm  
 $h_1 = \dots\dots\dots$  mm       $h = \dots\dots\dots$  mm

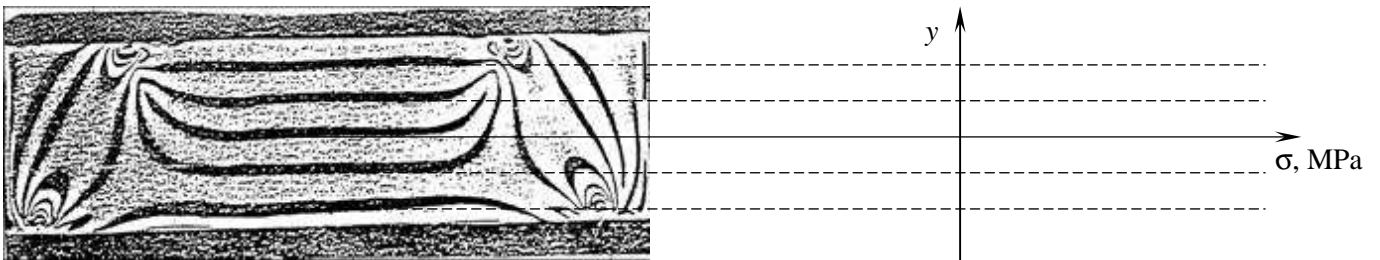
5) Experimental and calculation results:

Specimen:	Load level		Isochromatic fringe order at the notch tip - $m_{max}$	Stress concentration factor - $k_t$
	$2P$ , (scale)	$2P$ , (N)		
Model I				
Model II				

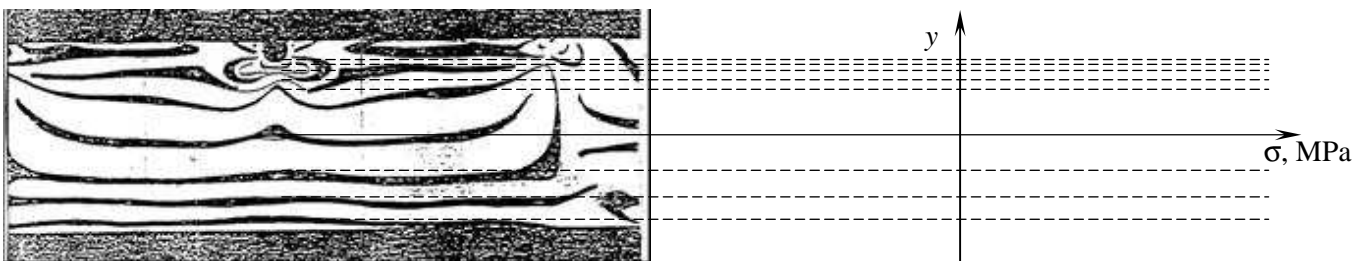
6) Stress distributions in the loaded by pure bending beam determined based isochromatic pattern fingers:

$K_{av} = \dots\dots\dots$  MPa ( acc. to Task No. 1.A)

a) The smooth beam:



b) The single notch beam:



c) The double notch beam:

